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(54) **PERFORMANCE ANALYSIS SYSTEM AND METHOD**

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G06F 19/00 (2006.01)
G06F 17/40 (2006.01)

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See application file for complete search history.

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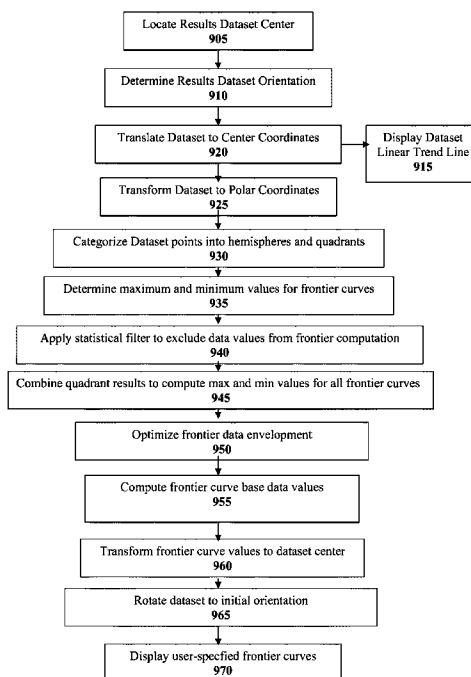
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(57) **ABSTRACT**

A system and method is described herein that includes a software-based functionality to assess the relationship between reliability, operational, maintenance and plant bet-terment activities and to determine the frontier of efficient spending and other measures of performance to achieve a level of reliability that is based on data from units of similar design and performance.

170 Claims, 4 Drawing Sheets



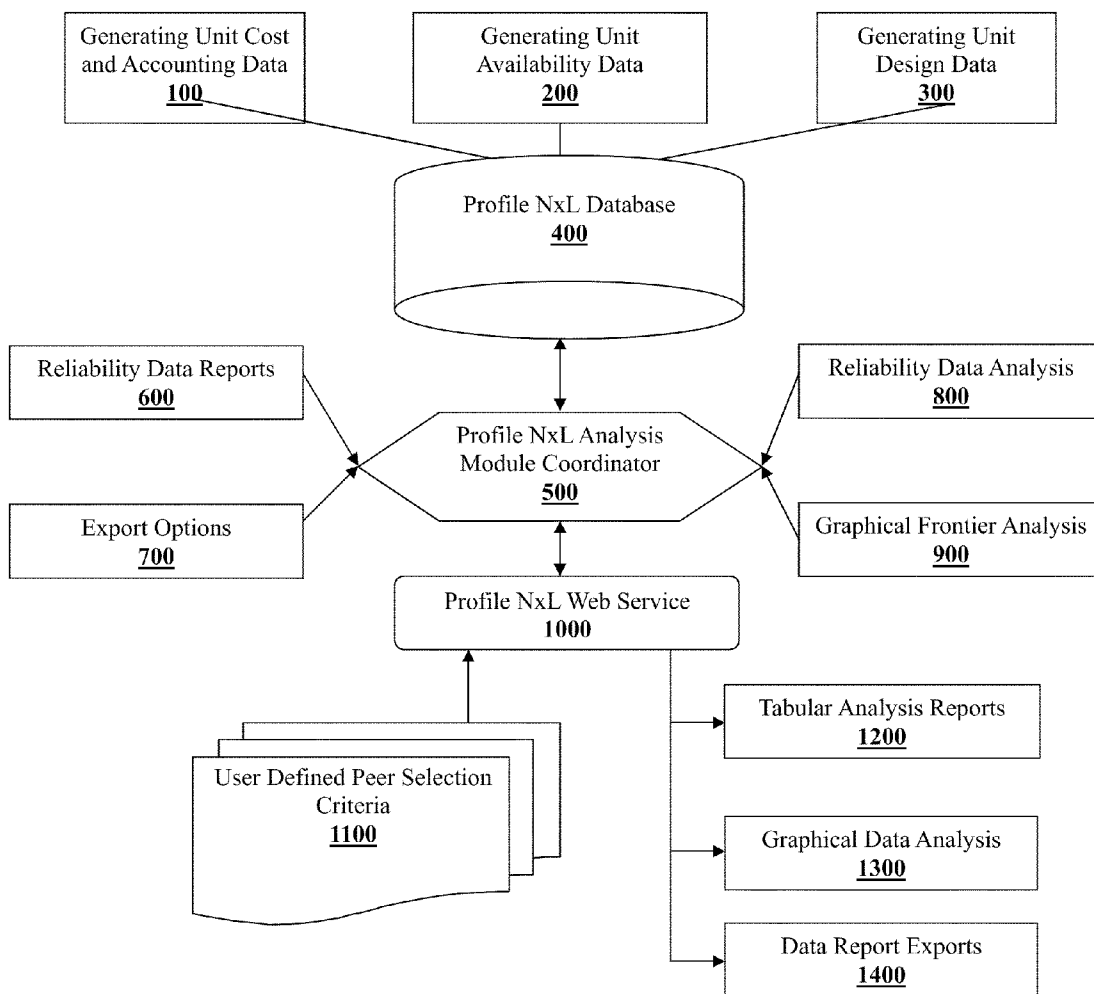


FIG. 1

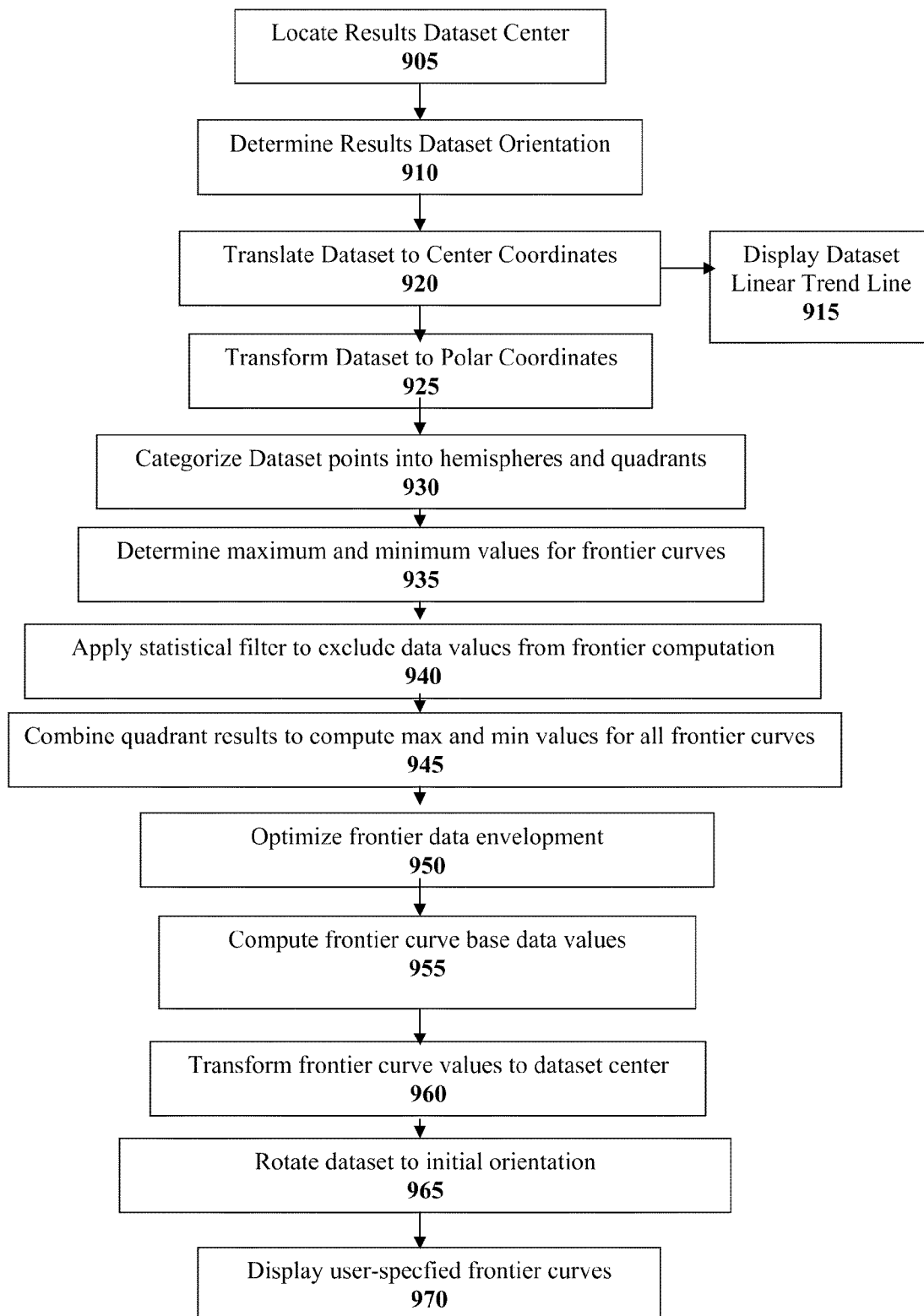


FIG. 2

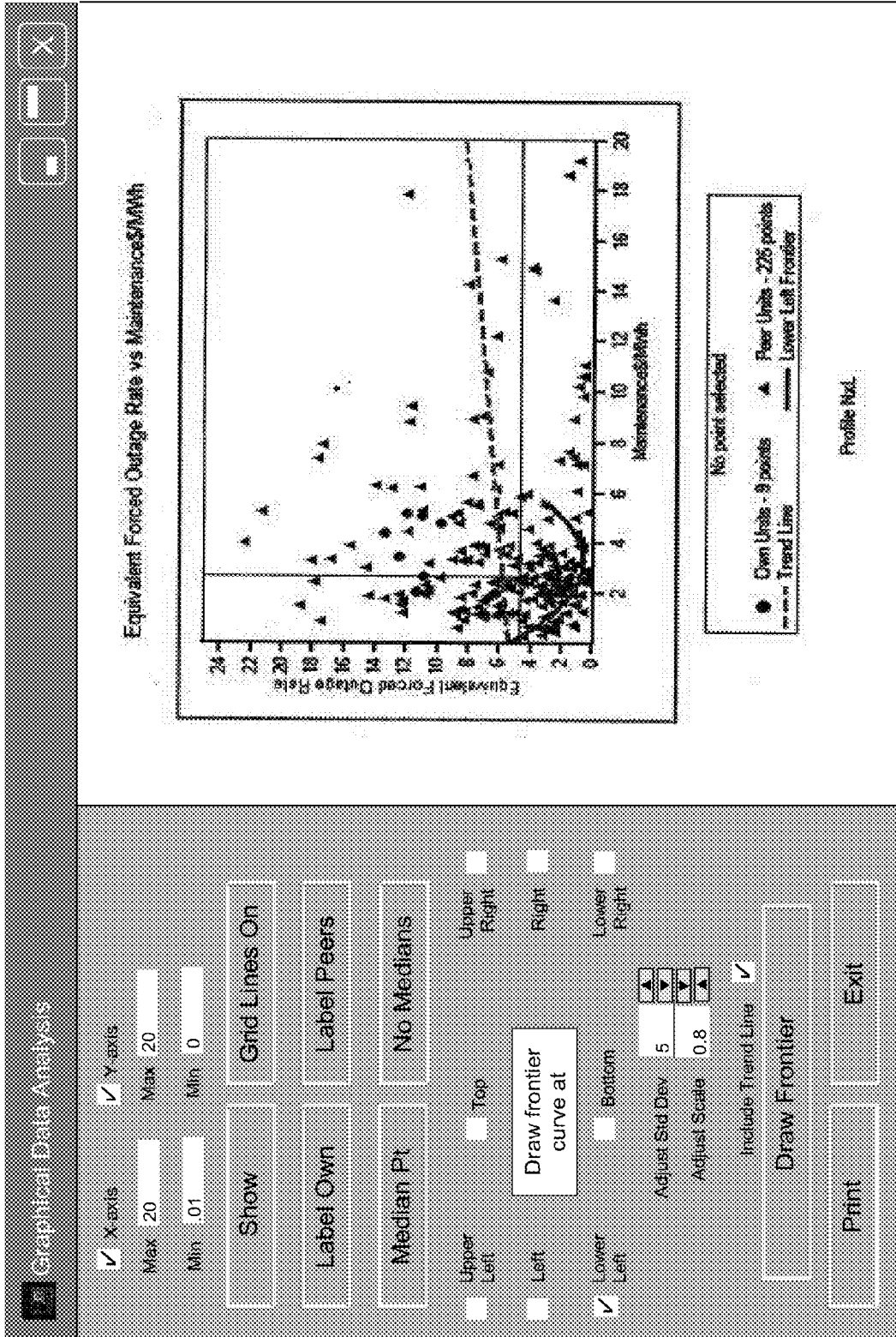


FIG. 3

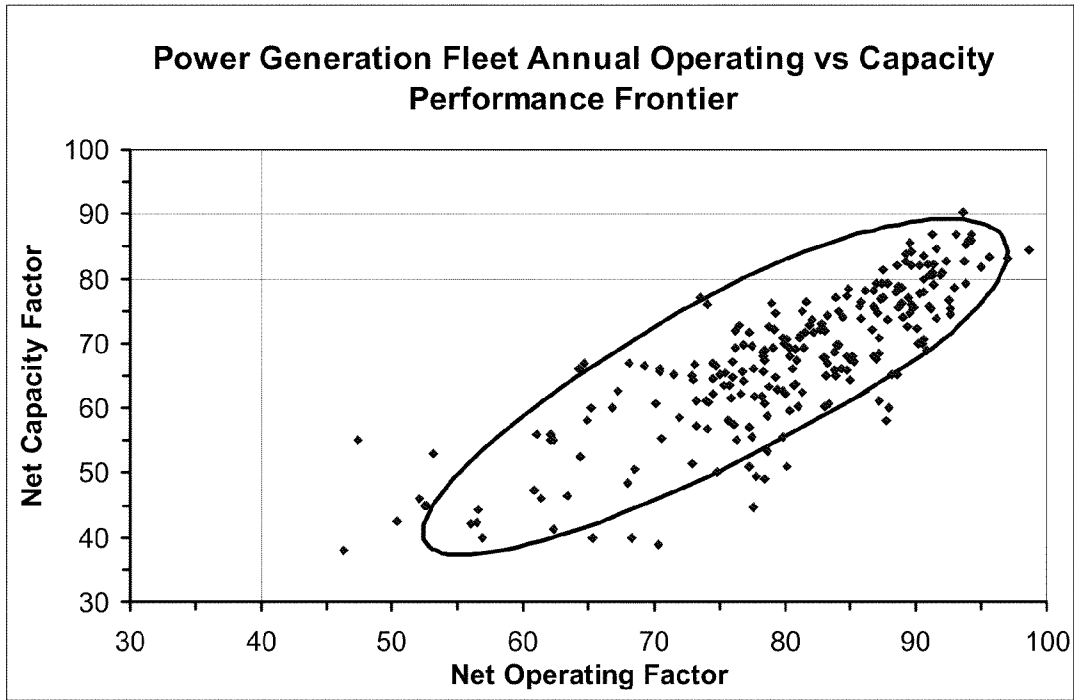


FIG. 4

PERFORMANCE ANALYSIS SYSTEM AND METHOD

CROSS-REFERENCE TO RELATED APPLICATIONS

This application is a continuation of U.S. patent application Ser. No. 11/801,221 filed May 9, 2007, now U.S. Pat. No. 7,447,611, which claims the benefits of expired U.S. Provisional Patent Application Ser. No. 60/798,924 filed May 9, 2006.

BACKGROUND OF THE INVENTION

1. Field of the Invention

The invention relates to a system and method for comparative operational performance analysis of one or more units, such as those used in industrial, power generation, pipeline, or refining facilities, using computer software, computer hardware, graphical presentation of results and statistical frontier analysis.

2. Background Summary

Negative competition requires that units perform in the most cost-effective manner consistent with their intended use. This means achieving strategic levels of realistic reliability and expenditures on a consistent basis. The cost-effective element of this relationship is the hardest to achieve. To be effective, a unit's reliability goals and expenditures must be matched with competitive expectations. Defining what constitutes competitive goals requires critical assessments and comparisons, which can best be done using statistical benchmarking techniques.

BRIEF SUMMARY OF THE INVENTION

What are the costs to maintain capacity, for example, an "available" or "reliable" kilowatt; and what are the correct, feasible and optimal targets to be set for each of the target units in this regard (i.e., cost efficiency)? The result is not a single point answer or a relationship that directly equates a given reliability level with a given expenditure. Rather, the result is a range of achievable reliability objectives and expenditure patterns containing the information needed to support unit-specific strategies. By way of example, applying the results of this methodology may be dependent upon the design characteristics, operating objectives as well as maintenance and plant betterment activities established for each unit.

Embodiments of the present invention provide a hardware and software tool, which overcome drawbacks of existing systems by providing a system and methodology for estimating a generating unit's potential reliability and cost that enables dynamic analyses. The predictive system and methodology of this embodiment is based on an evaluation of the relationship of unit reliability with key parameters, such as unit design characteristics, operational factors, maintenance, and plant betterment activities. While the detailed embodiments described herein deal with the power generation industry, these embodiments are illustrative and exemplary only, since the present invention may be used in numerous types of facilities, including but not limited to: refining, pipeline, chemical, industrial, pharmaceutical, healthcare, agricultural, environmental, offshore energy production, and educational facilities.

An embodiment of the present invention includes a method for generating a complete frontier curve comprising the steps of: providing a dataset of user-selected data corresponding to

a plurality of reference units, the user-selected data comprising a plurality of variables; and computing a complete frontier curve for a user-selected dataset corresponding to at least one of the plurality of variables.

Another embodiment of the present invention includes a method for providing dynamic comparative operational performance analyses comprising the steps of: providing a dataset of user-selected data corresponding to a plurality of reference power generating units, the user-selected data comprising a plurality of variables; computing a complete frontier curve for a user-selected dataset corresponding to at least one of the plurality of variables; and comparing data corresponding to a target unit to a portion of the complete frontier curve.

Another embodiment of the present invention includes a system comprising: a server, comprising: a processor, and a storage subsystem: a database stored by the storage subsystem comprising: a plurality of data corresponding to reference units; and a computer program stored by the storage subsystem that, when executed, causes the processor to: select a dataset from the plurality of data corresponding to user selection criteria; and determine a complete frontier curve based on the dataset.

It is expressly within the scope of the disclosed and claimed present invention that one or more steps or limitations of the present invention may be performed by a third party.

Several determinations are based on the geometric center, instead of direct calculation, since the method includes the filtering of data points, and, as necessary, data points may be eliminated from a calculation if it is determined that the data points would lead to a frontier curve that did not accurately reflect the data as a whole.

BRIEF DESCRIPTION OF THE DRAWINGS

A better understanding of the present invention can be obtained when the following detailed description of the preferred embodiment is considered in conjunction with the following drawings, in which:

FIG. 1 is a block diagram of components for the claimed product, system, and method.

FIG. 2 is a flowchart of an embodiment of the claimed product, system, and method.

FIG. 3 is a screen shot of a frontier curve in an embodiment of the claimed product, system, and method.

FIG. 4 is a screen shot of a complete frontier curve in an embodiment of the claimed product, system, and method.

DETAILED DESCRIPTION OF EMBODIMENTS OF THE INVENTION

As shown in FIG. 1, the Performance Analysis System and Method according to one embodiment of the present invention is shown. While embodiments of the invention are described in terms of power generating units by way of example, the invention is not restricted to power generating facilities, but encompasses other types of facilities including, but not limited to, refining, pipeline, chemical, industrial, pharmaceutical, healthcare, agricultural, environmental, offshore energy production, and educational facilities. Operational and cost data for generating units, where the design characteristics are known at a level of granularity consistent with the analysis goals, serve as the basic input for this invention. Cost data **100** generally includes monies for operations, fuel, maintenance, and capital improvements. The data is consistent with the level of detail available in the reliability

data (e.g., components, subsystems, systems and unit) and with the granularity of the reported reliability data (i.e., monthly).

The operational availability data **200** is composed of event and performance information. The event database is a detailed summary of the outage and derating events each unit had during any given period. Summarized on a monthly basis, the performance database includes capacity ratings, generation, loading modes, availability and unavailability hours, and fuel quality information for each unit.

The Generating Unit Design **300** database in this embodiment consists of details on the design parameters and installed equipment on each unit.

The integrated data is stored in a database **400**. This database **400** in this embodiment serves as the primary data source for all calculations and analysis. It is accessed by an analysis controller **500** that coordinates what specific calculations are requested by a user in this embodiment.

The analysis modules in this embodiment include reliability data analysis reports **600** which list the desired reliability metrics in a user-specified format.

The export options module **700** enables users to transfer data and reports from this system to other user-specified systems for extended analyses in this embodiment.

The reliability data analysis module **800** computes user-specific summary metrics and indices including but not limited to monthly, period average, or period total unitized cost data (\$ per kW or per MWh) and reliability measures for the peer-unit group that includes the target unit(s) only, the peer-unit group including the target unit(s), or the peer-unit group excluding the target unit(s).

The Graphical Frontier Analysis Module **900** enables users to review various strategies assists the decision-making process in setting realistic unit performance targets based on data from actual achieved performance by units in the comparison analysis as selected by the user.

As shown in FIG. 2, a pre-selected dataset, called the results dataset, is used and its geometric center is determined in step **905**. The conversion of the results dataset from its initial orientation, as determined in step **905**, to polar coordinates takes place in step **920** and step **925**. The use of polar coordinates is illustrative and exemplary only. The orientation of the results dataset is analyzed in step **910** and transformations are applied in step **920** and a linear trend is displayed in step **915**. The results dataset is further transformed to polar coordinates in **925** and data values are categorized into hemispheres and quadrants in step **930**. The methodology does not arbitrarily eliminate any generating unit that might have experienced an abnormal occurrence (data outlier); this might, in itself, bias the results. As an example, a generating unit's Equivalent Forced Outage Rate (EFOR) or expenditure pattern may be extremely high or low for one of the study periods and more reasonable at others. Excluding this high/low period would bias the analysis. Graphical data analysis allows the user to be aware of these extremes and subjective interpretations of these graphs could easily consider them. The resultant dataset's maxima and minima are computed in step **935**, which provides maximum and minimum values for frontier curves. A statistical filter is applied in step **940** to determine which data values will be used in the frontier calculation. Based on user-specified inputs, the data is combined into frontier groups and new maxima and minima are calculated for composite frontier curves in step **945**. The complete frontier curve is composed of the individual frontier curves (i.e. left hemisphere, right hemisphere, top hemisphere, bottom hemisphere, upper right quadrant, lower right quadrant, upper left quadrant, lower left quadrant)

for a variable. These complete frontier curves are further refined to contain the maximum data envelopment in step **950**. The frontier data groups are used to compute nonlinear complete frontier curves in step **955**. The complete frontier curves are converted back to their original orientation in step **960** and step **965**. The complete frontier curves are then transformed to the results dataset center in step **960**, re-rotated to initial orientation in step **965**, and displayed in graphical format superimposed on the detailed results dataset plot in step **970**. The order of the foregoing steps in this embodiment is illustrative and exemplary, and the method may be practiced with the steps in a different order and may be performed using individual frontier curves.

The interface between users world-wide is managed by the Profile NxL web service in **1000**. This interface performs functions related to data security and information management between the database and the family of independent users.

User selected target units to be benchmarked **1100** and the peer-unit group that has similar design characteristics and operational parameters of the target unit to the experience data contained in the database **400** are compared.

Users may select the report format and structure for which would like to view certain results **1200**.

The graphical output **1300** is shown in FIG. 3. It is a dynamic framework that enables users to continuously select new result sets and re-analyze and re-compare their units' performance. This integrated statistical graphical presentation is a part of the invention that enables users to re-select and thereby refine, their results set to more precisely define their performance peer group.

While FIG. 3 displays an individual frontier curve as the graphical output **1300**, FIG. 4 displays a complete frontier curve, wherein the complete frontier curve is formed by combining a plurality of individual frontier curves.

Example #1

In one embodiment of the invention, the user can extract either monthly, period average, or period total unitized cost data (\$ per kW or per MWh) and reliability measures for the peer-unit group that includes the target unit(s) only, the peer-unit group including the target unit(s), or the peer-unit group excluding the target unit(s). After tabulation and analysis of the resultant reliability and cost data, the user may prepare graphs showing unitized costs versus an appropriate reliability measure. The user may draw median lines for the unitized costs and reliability measure values to establish four distinct quadrants as shown in FIG. 3. The methodology in this example includes two statistical-based views of the data: (1) using the quadrant diagram, determining the trend line for the data to determine the change in the reliability measure per incremental change in unitized cost, and (2) using the quadrant diagram, performing the Frontier Analysis for the appropriate section of the data (i.e., the "best-performance" quadrant or side of the dataset) where the sections are identified as: quadrant (upper-right, upper-left, lower-right, and lower-left) or side (top, bottom, left, and right). The graphical analysis technique included in this invention in one embodiment, allows the analysis of monthly, period average, and period total values using quadrants. In this embodiment, quadrants are formed when, a horizontal line is drawn at the median of the y-axis value and a vertical line is drawn at the median of the x-axis value. The resulting "cross-hair" pattern allows the units to be divided into quadrants as in FIG. 3. Each quadrant can be seen to represent different operating and expenditure strategies. This use of medians for each axis and quadrants is

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illustrative and exemplary only and other lines may be used. For example, several lines may be used to on each axis to create a grid separating data points into highly specific groups. Changes in spending and operating strategies could be observed using multi-year rolling averages by reviewing graphs for several successive multi-year periods.

In FIG. 3, the quadrants created in the embodiment provide an indicator to the user of the performance of the target units compared with the dataset of units overall. In this embodiment, units with below median maintenance/\$MWH and below median EFOR appear in the lower left quadrant. Units performing above the median in maintenance/\$MWH and EFOR appear in the upper right quadrant. In this embodiment, a least squares fit is provided for all of the units and displayed as a dashed line. In this embodiment, frontier curves may be selected for viewing. Each frontier curve is calculated to envelope an optimal portion of the dataset while excluding extreme values (outliers). The decision of whether a point is an outlier is based on a statistical determination. In this embodiment, frontier curves may be displayed for any quadrant or to either side of either of the median lines. This display is illustrative and exemplary only.

The methodology shows that the benchmarking analysis varies with the inherent design and historical operating characteristics associated with the target unit(s). It also shows that operations and maintenance costs and plant betterment activities vary and are dependent on the strategies assigned to each generating unit. It demonstrates that given nearly any set of circumstances, changes can be made affecting generating unit reliability, costs, or both. In effect, by applying the methodology and making informed decisions, plant generation managers can set realistic, data-based performance targets.

The methodology simultaneously considers the impact of design and operational variables on the performance of an electric generating unit. The design characteristics and operational factors of the target unit(s) are the focus of this methodology. This results in the identification of a statistically valid group of units that have similar traits. Within the peer unit grouping, the units are not all the same, but they are not different enough to be different.

There are many viewpoints on which design characteristics and operation variables impact generating units. This methodology allows the user to use their own knowledge of which variables impact reliability. The benchmarking list includes two types of variables: class and continuous. Class-types include variables such as: criticality (supercritical versus sub-critical), balanced versus pressurized furnace draft, number of reheats, etc. These are yes/no-type variables. Examples of continuous-type variables include: unit capacity ratings (generally between 1 and 1,200 MWe), reserve shutdown hours (generally between 0 and 8,784 hours), and unit age or vintage period based on year of installation. These are range-type variables.

The dynamic nature of this invention allows users to identify key factors influencing performance. The procedure can be applied to general unit types or tailored to a specific generating unit. The result is a more focused peer unit group against which comparisons can be made.

Users can select specific reporting metrics and analysis indices to be included in the data reports either for used within this invention or for exporting 1400 to other software for additional analyses.

Example #2

The present invention is used to generate one or more frontier curves or a complete frontier curve to benchmark the

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refining industry. Refining variables may be input into the database, such as maintenance costs, throughput, geographic location, product type, labor costs, facility availability percentage, and maximum capacity.

From these variables, a frontier curve is generated determining, by way of example, cost efficiency per unit product, product per unit cost, and facility availability percentage relative to maintenance costs. Reference units, such as a reference refining unit, are constructed from the input variables and used to establish benchmarks for comparison with target refining units.

Example #3

The present invention is used to generate one or more frontier curves or a complete frontier curve to benchmark the pipeline industry. Pipeline variables may be input into the database, such as engine maintenance costs, throughput, compression type, turbine starts, rights-of-way costs, land leases, population density, environmental costs, total installed horsepower, number of engines, pipeline segment length, pipeline diameter, storage capacity, and fuel costs.

From these variables a frontier curve is generated determining, by way of example, best usage of fuel per unit horsepower, overall performance by pipeline segment, pipeline expansion cost effectiveness, and maintenance and environmental costs dependent on population density. Reference units, such as a reference pipeline, are constructed from the input variables and used to establish benchmarks for comparison with target pipelines.

Example #4

The present invention is used to generate one or more frontier curves or a complete frontier curve to benchmark the chemical industry. Chemical variables may be input into the database, such as size and number of reactor vessels, usage rates for raw materials, production rates per product, storage capacity, energy usage, carbon emissions, plant availability percentage, maintenance costs, safety costs, accident rates, and automation costs.

From these variables a frontier curve is generated determining, by way of example, accident rates increase/decrease with safety budget, plant availability percentage increase/decrease with automation costs, identify lowest emissions facilities, and carbon emissions increase/decrease with maintenance costs. Reference units, such as a reference chemical plant, are constructed from the input variables and used to establish benchmarks for comparison with target chemical plant.

Example #5

The present invention is used to generate one or more frontier curves or a complete frontier curve to benchmark the industrial facilities. Industrial variables may be input into the database, such as plant safety, product quality, manufacturing schedules, delivery schedules, accounts receivables, maintenance costs, gross profits, and revenue.

From these variables a frontier curve is generated determining, by way of example, gross profit impact due to maintenance costs, revenue increase/decrease relative to product quality, and plant safety increase/decrease compared with maintenance costs. Reference units, such as a reference industrial plant, are constructed from the input variables and used to establish benchmarks for comparison with target industrial plant.

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Example #6

The present invention is used to generate one or more frontier curves or a complete frontier curve to benchmark the pharmaceutical industry. Pharmaceutical variables may be input into the database, such as plant safety, batch quality, number of batches, actual yields, number of processes, dose size production, manufacturing schedules, ingredient stocks, ingredient suppliers, recalls, work shifts, and maintenance costs.

From these variables a frontier curve is generated determining, by way of example, batch failure rate increase/decrease with ingredient suppliers, maintenance costs impact due to number of processes, and batch quality increase/decrease by work shift. The manager can decide if one shift's performance exceeds the other or that they can be judged the same. Other frontier analyses could involve for example, the highest cycle times and the lowest number of batches failed, and the lowest cycle times and the highest yields. Reference units, such as a reference pharmaceutical plant, are constructed from the input variables and used to establish benchmarks for comparison with target pharmaceutical plant.

Example #7

The present invention is used to generate one or more frontier curves or a complete frontier curve to benchmark the healthcare industry. Healthcare variables may be input into the database, such as total cost of service per year, total expenditure on non-labor inputs, total administrative costs, cost of purchased services, number of patients treated per year by patient category, average length of patient stay, average age of patients, area of specialization, average severity of cases, relative weight of caseload, physician's average age, fraction of caseload with satisfactory outcomes, nursing staff hourly wages, hourly wage for physicians and other professional staff, hourly wage for all other staff, number of beds, number of medical doctors, registered nurses, nonregistered nurses, nurse trainees, therapists, general and other staff, occupancy rate, proportion of patients older than 65, Medicare, Medicaid, private and other patient days, percentage of doctors on staff, rate of hospital admissions per 1000 population, unionization, level of malpractice premiums, percentage of visits using lab tests or x-rays, years of physician experience, number of physicians per 1000 county population, population density, number of acute-care beds, number of long-term beds, number of emergency visits, proportion of female patients, teaching facilities, or any other variable to be analyzed.

From these variables, a frontier curve is generated determining, by way of example, for-profit hospitals more/less efficient than not-for-profit hospitals; public hospitals less/more efficient than private hospitals; facilities with larger Medicare populations and number of beds more/less efficient; unionization or excess bed capacity add significantly to hospital costs; government-controlled hospitals more/less efficient; hospitals in highly competitive, population- and physician-dense areas more/less efficient; greater expenditures on administration and nursing staff associated with higher efficiency; and are HMO type, profit status, federal eligibility and age predictive variables for efficiency. Reference units, such as a reference hospital, are constructed from the input variables and used to establish benchmarks for comparison with target hospitals or clinics.

Example #8

The present invention is used to generate one or more frontier curves or a complete frontier curve to benchmark in

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the agricultural industry. Agricultural variables may be input into the database, such as land (area dedicated to crops), quantity produced and actually harvested by grain type, labor by type (household labor, permanent and temporary employees, partners and other sources of farm labor), machines, types of fertilizers and nutrient contents, types of pesticides, grain types planted, seeds and seedlings, land rental rates and monthly salaries paid wage earners, types of mechanization available, stocks of tractors and harvesters, available irrigation and water resources, average temperature, average rainfall, degree days compared to a standard measure, length of growing season, altitude, latitude, country, and region, or any other variable to be analyzed.

From these variables, a frontier curve is generated determining, by way of example, estimates of what the crop production might have been if all producers used the same levels of inputs but used them efficiently. More specifically, for example, region A could have produced 5.4% more, and region B could have boosted output by 96.5%. Can technical efficiency be explained primarily by soil and climatic conditions and irrigation? If, for example, all regional agricultural producers were to produce at the technically efficiency frontier, the nation/regional crop production could increase by more than 30%. Reference units, such as reference farms or regions, are constructed from the input variables and used to establish benchmarks for comparison with target farms or regions.

Example #9

The present invention is used to generate one or more frontier curves or a complete frontier curve to benchmark the field of environmental protection and monitoring. The primary variables include measures of human activity and indicators of forest and rangeland conditions in place of the more traditional economic inputs (costs) and outputs such as: ratio of area of disturbed land to total area, total linear edge between natural land cover and human land use, ratio of average patch size to the maximum possible, proportion of endangered species to total individual species, mortality in growing stock on timberlands, ratio of actual productivity on timberlands to potential productivity, absolute value of the difference between recent stream flow and historical average, total nitrogen measured in surface waters, maximum pH in precipitation minus observed pH in precipitation, total phosphorous measured in surface waters, total toxic chemical releases to the environment (air, water, and land), proportion of area that is designated as protected, human population density, dam density, beef cattle density, mining density, productive oil and gas well density, timber harvest, road density, outdoor recreation activity measures, total farm production, mean annual temperature, spatial variation in temperature, seasonal variation in temperature, mean annual precipitation, seasonal variation in precipitation, spatial variation in precipitation, total vegetation carbon, or any other variable to be analyzed. These variables would be collected by country and region/county.

A frontier curve is generated determining, by way of example, areas in a country where there is maximum potential for improving the forest and rangeland condition, based on various indicator variables; what could be reasonably and realistically achievable in determining/forecasting the potential impact on forest and rangelands by increasing recreational use of these areas, expanding or reducing rangelands for cattle grazing, opening areas to drilling, and harvesting timber in national forest and grasslands. Reference units, such as reference counties or regions, are constructed from

the input variables and used to establish benchmarks for comparison with target farms or regions.

Example #10

The present invention is used to generate one or more frontier curves or a complete frontier curve to benchmarking the offshore energy production industry. The database could include offshore exploration, development, and production data such as offshore drilling costs grouped by depth intervals, operating costs for each platform, monthly oil, gas, and produced water outputs from every well in a region by year; borehole data describing drilling activity for each well; platform data such as size (i.e., slots) and water depth for each platform including substructures; field reserve data including oil and gas reserve sizes and discovery year for each field; and reservoir-level porosity information/measurements. The database could also be comprised of well-level data for oil output, gas output, produced water output, and the quantity of fluid injected, and field-level data for the number of exploration wells drilled, total drilling distance of exploration wells, total vertical distance of exploration wells, number of development wells drilled, total drilling distance of development wells, total vertical distance of development wells, number of platforms, total number of slots, total number of slots drilled, water depth, oil reserves, gas reserves, original proved oil and gas combined reserves, number of environmental regulations, environmental compliance costs, environmental emission data including water pollutants, discovery year, porosity, or any other variable to be analyzed.

The frontier curves are generated to determine, by way of example, the effect of technological change on the offshore energy production industry at the field level over time; the impact of water depth (drilling wells in deeper waters); the impact (significant or insignificant) on offshore production resulting from environmental regulation; changes in production efficiency at the field level due to depletion of reserves and resulting expansion of exploration and production in deep waters; and impacts over time due to technological change and improvement in management. Reference units, such as reference wells or platforms, are constructed from input variable and used to establish benchmarks for comparison with target wells and platforms.

Example #11

The present invention is used to generate one or more frontier curves or a complete frontier curve to benchmark educational systems. The database could include annual data on each school: school district, state, population in district, average family income in district, average level of education of school district population, average performance on several standardized tests by grade level, number of classroom days in the school year, instructional expenditures per student, other expenditures per student, average teacher salary, average years of experience for teachers, proportion of teachers having and advanced degree, student-teacher ratio, total enrollment in school, percent of students eligible for subsidized lunches, percent minority students, percent of students classified as possessing English proficiency (e.g., English as a secondary language), number of teachers, number of teacher aides, ratio of administrative staff to teaching staff, expenditures per student for administrative and other school operations, district school taxes per student, average administrative salary, or any other variable to be analyzed.

From these variables, the frontier curve generated determines, by way of example, impact of spending on student test

scores on the standardized tests; impact of reducing non-instructional and shifting to instructional spending on academic achievement for a given grade level; impediments to learning created by the environment for schools with higher percentages of disadvantaged students; effects on academic achievement due to increasing or freezing teacher salaries, increasing class sizes, or providing teachers with teaching aides; effects of district or school size on efficiency of school districts. Reference units, such as classes, schools, and colleges, are constructed from the input variables and used to establish benchmarks for comparison with target classes, schools, and colleges.

The foregoing disclosure and description of various embodiments of the invention are illustrative and explanatory thereof, and various changes in the details of the illustrated system and method may be made without departing from the scope of the invention.

We claim:

1. A method for generating a complete frontier curve comprising the steps of:

providing a dataset of user-selected data comprising a plurality of variables;

converting the dataset to a geometric coordinate system;

computing a complete frontier curve for a user-selected dataset corresponding to at least one of the plurality of variables.

2. The method of claim 1, further comprising the step of: comparing data corresponding to a target unit to a portion of the complete frontier curve.

3. The method of claim 1, wherein the user-selected data corresponds to a plurality of reference units, and wherein the plurality of units is selected from a set of unit types consisting of:

power generating, refining, pipeline, chemical, industrial, pharmaceutical, healthcare, agricultural, environmental, offshore, and educational units.

4. The method of claim 1, wherein converting the dataset further comprises the steps of:

determining an initial orientation for the dataset; and rotating the dataset to a predetermined orientation.

5. The method of claim 1, wherein computing a complete frontier curve further comprises the step of:

computing maximum and minimum values for the variables of the dataset.

6. The method of claim 1, further comprising the step of displaying a linear trend of the dataset.

7. The method of claim 1, further comprising the step of displaying a linear trend of the dataset.

8. The method of claim 1, wherein the plurality of variables comprises one or more of unit design characteristics, operations factors, and maintenance and plant betterment data, or combinations thereof.

9. The method of claim 1, wherein the target unit is a reference unit.

10. The method of claim 1 wherein computing a complete frontier curve comprises the step of:

combining data from the dataset into a plurality of frontier groups.

11. The method of claim 10, wherein computing a complete frontier curve further comprises the step of:

filtering the dataset; and

computing the complete frontier curve from the plurality of frontier groups.

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12. The method of claim **1**, wherein converting the dataset comprises the step of:

determining an initial orientation for the dataset; and wherein computing the complete frontier curve further comprises the step of reorienting the complete frontier curve to the initial orientation. 5

13. The method of claim **12**, wherein reorienting the complete frontier curve comprises the steps of:

transforming the complete frontier curve to the dataset center; and rotating the complete frontier curve to the initial orientation. 10

14. The method of claim **1**, wherein computing a complete frontier curve further comprises the steps of:

categorizing data from the dataset into hemispheres and quadrants; 15

computing maxima and minima for the variables of the dataset;

computing a plurality of frontier curves corresponding to the hemispheres and quadrants; 20

statistically filtering the dataset; combining the variables into frontier groups, creating composite frontier curves;

computing maxima and minima for the composite frontier curves; and 25

combining the composite frontier curves into a complete frontier curve.

15. The method of claim **14**, wherein statistically filtering the dataset comprises the step of

removing outlier data points. 30

16. A method for generating a complete frontier curve comprising the steps of:

providing a dataset of user-selected data corresponding to a plurality of reference refining units, the user-selected data comprising a plurality of variables, 35

wherein the plurality of variables comprises one or more of maintenance costs, throughput, geographic location, product type, labor costs, facility availability percentage, and maximum capacity;

converting the dataset to a geometric coordinate system; 40

computing a complete frontier curve for a user-selected dataset corresponding to at least one of the plurality of variables; and

comparing data corresponding to a target unit to a portion of the complete frontier curve. 45

17. The method of claim **16**, wherein converting the dataset further comprises the steps of:

determining an initial orientation for the dataset; and rotating the dataset to a predetermined orientation.

18. The method of claim **16**, wherein computing a complete frontier curve further comprises the step of: 50

computing maximum and minimum values for the variables of the dataset.

19. The method of claim **16**, further comprising the step of displaying a linear trend of the dataset. 55

20. The method of claim **16**, further comprising the step of displaying the complete frontier curve.

21. The method of claim **16**, wherein the plurality of variables comprises one or more of unit design characteristics, operations factors, and maintenance and plant betterment data, or combinations thereof. 60

22. The method of claim **16**, wherein the target unit is a reference refining unit.

23. The method of claim **16** wherein computing a complete frontier curve comprises the step of: 65

combining data from the dataset into a plurality of frontier groups.

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24. The method of claim **23**, wherein computing a complete frontier curve further comprises the step of:

filtering the dataset; and

computing the complete frontier curve from the plurality of frontier groups.

25. The method of claim **16**, wherein converting the dataset comprises the step of:

determining an initial orientation for the dataset; and

wherein computing the complete frontier curve further comprises the step of reorienting the complete frontier curve to the initial orientation.

26. The method of claim **25**, wherein reorienting the complete frontier curve comprises the steps of:

transforming the complete frontier curve to the dataset center; and rotating the complete frontier curve to the initial orientation.

27. The method of claim **16**, wherein computing a complete frontier curve further comprises the steps of:

categorizing data from the dataset into hemispheres and quadrants;

computing maxima and minima for the variables of the dataset;

computing a plurality of frontier curves corresponding to the hemispheres and quadrants; 20

statistically filtering the dataset;

combining the variables into frontier groups, creating composite frontier curves;

computing maxima and minima for the composite frontier curves; and 25

combining the composite frontier curves into a complete frontier curve.

28. The method of claim **27**, wherein statistically filtering the dataset comprises the step of:

removing outlier data points. 35

29. A method for generating a complete frontier curve comprising the steps of:

providing a dataset of user-selected data corresponding to a plurality of reference pipeline units, the user-selected data comprising a plurality of variables, 40

wherein the plurality of variables comprises one or more of:

engine maintenance costs, throughput, compression type, turbine starts, rights-of-way costs, land leases, population density, environmental costs, total installed horsepower, number of engines, pipeline segment length, pipeline diameter, storage capacity, and fuel costs; 45

converting the dataset to a geometric coordinate system;

computing a complete frontier curve for a user-selected dataset corresponding to at least one of the plurality of variables; and

comparing data corresponding to a target unit to a portion of the complete frontier curve. 50

30. The method of claim **29**, wherein converting the dataset further comprises the steps of:

determining an initial orientation for the dataset; and rotating the dataset to a predetermined orientation.

31. The method of claim **29**, wherein computing a complete frontier curve further comprises the step of:

computing maximum and minimum values for the variables of the dataset.

32. The method of claim **25**, further comprising the step of: displaying a linear trend of the dataset. 55

33. The method of claim **25**, further comprising the step of displaying the complete frontier curve.

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34. The method of claim 25, wherein the plurality of variables comprises one or more of unit design characteristics, operations factors, and maintenance and plant betterment data, or combinations thereof.

35. The method of claim 25, wherein the target unit is a reference unit.

36. The method of claim 25, wherein the target unit is a reference pipeline unit.

37. The method of claim 29 wherein computing a complete frontier curve comprises the step of:

combining data from the dataset into a plurality of frontier groups.

38. The method of claim 37, wherein computing a complete frontier curve further comprises the step of:

filtering the dataset; and

computing the complete frontier curve from the plurality of frontier groups.

39. The method of claim 29, wherein converting the dataset comprises the step of:

determining an initial orientation for the dataset; and

wherein computing the complete frontier curve further comprises the step of:

reorienting the complete frontier curve to the initial orientation.

40. The method of claim 39, wherein reorienting the complete frontier curve comprises the steps of:

transforming the complete frontier curve to the dataset center; and rotating the complete frontier curve to the initial orientation.

41. The method of claim 29, wherein computing a complete frontier curve further comprises the steps of:

categorizing data from the dataset into hemispheres and quadrants;

computing maxima and minima for the variables of the dataset;

computing a plurality of frontier curves corresponding to the hemispheres and quadrants;

statistically filtering the dataset;

combining the variables into frontier groups, creating composite frontier curves;

computing maxima and minima for the composite frontier curves; and

combining the composite frontier curves into a complete frontier curve.

42. The method of claim 41, wherein statistically filtering the dataset comprises the step of:

removing outlier data points.

43. A method for generating a complete frontier curve comprising the steps of:

providing a dataset of user-selected data corresponding to a plurality of reference chemical units, the user-selected data comprising a plurality of variables, wherein the plurality of variables comprises one or more of:

size of reactor vessels, number of reactor vessels, usage rates for raw materials, production rates per product, storage capacity, energy usage, carbon emissions, plant availability percentage, maintenance costs, safety costs, accident rates, and automation costs;

converting the dataset to a geometric coordinate system; computing a complete frontier curve for a user-selected dataset corresponding to at least one of the plurality of variables; and

comparing data corresponding to a target unit to a portion of the complete frontier curve.

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44. The method of claim 43, wherein converting the dataset further comprises the steps of:

determining an initial orientation for the dataset; and rotating the dataset to a predetermined orientation.

45. The method of claim 43, wherein computing a complete frontier curve further comprises the step of:

computing maximum and minimum values for the variables of the dataset.

46. The method of claim 43, further comprising the step of displaying a linear trend of the dataset.

47. The method of claim 43, further comprising the step of displaying the complete frontier curve.

48. The method of claim 43, wherein the plurality of variables comprises one or more of unit design characteristics, operations factors, and maintenance and plant betterment data, or combinations thereof.

49. The method of claim 43, wherein the target unit is a reference chemical unit.

50. The method of claim 43 wherein computing a complete frontier curve comprises the step of:

combining data from the dataset into a plurality of frontier groups.

51. The method of claim 50, wherein computing a complete frontier curve further comprises the step of:

filtering the dataset; and

computing the complete frontier curve from the plurality of frontier groups.

52. The method of claim 43, wherein converting the dataset comprises the step of:

determining an initial orientation for the dataset; and

wherein computing the complete frontier curve further comprises the step of reorienting the complete frontier curve to the initial orientation.

53. The method of claim 52, wherein reorienting the complete frontier curve comprises the steps of:

transforming the complete frontier curve to the dataset center; and

rotating the complete frontier curve to the initial orientation.

54. The method of claim 43, wherein computing a complete frontier curve further comprises the steps of:

categorizing data from the dataset into hemispheres and quadrants;

computing maxima and minima for the variables of the dataset;

computing a plurality of frontier curves corresponding to the hemispheres and quadrants;

statistically filtering the dataset;

combining the variables into frontier groups, creating composite frontier curves;

computing maxima and minima for the composite frontier curves; and

combining the composite frontier curves into a complete frontier curve.

55. The method of claim 54, wherein statistically filtering the dataset comprises the step of:

removing outlier data points.

56. A method for generating a complete frontier curve comprising the steps of:

providing a dataset of user-selected data corresponding to a plurality of reference industrial units, the user-selected data comprising a plurality of variables,

wherein the plurality of variables comprises one or more of:

accident rate, product quality, manufacturing schedules, delivery schedules, accounts receivables, maintenance costs, gross profits, and revenue;

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converting the dataset to a geometric coordinate system;
 computing a complete frontier curve for a user-selected
 dataset corresponding to at least one of the plurality of
 variables; and

comparing data corresponding to a target unit to a portion
 of the complete frontier curve.

57. The method of claim **56**, wherein converting the dataset
 further comprises the steps of:

determining an initial orientation for the dataset; and
 rotating the dataset to a predetermined orientation.

58. The method of claim **56**, wherein computing a complete
 frontier curve further comprises the step of:

computing maximum and minimum values for the variables
 of the dataset.

59. The method of claim **56**, further comprising the step of:
 displaying a linear trend of the dataset.

60. The method of claim **56**, further comprising the step of:
 displaying the complete frontier curve.

61. The method of claim **56**, wherein the plurality of variables
 comprises one or more of unit design characteristics,
 operations factors, and maintenance and plant betterment
 data, or combinations thereof.

62. The method of claim **56**, wherein the target unit is a
 reference industrial unit.

63. The method of claim **56** wherein computing a complete
 frontier curve comprises the step of

combining data from the dataset into a plurality of frontier
 groups.

64. The method of claim **63**, wherein computing a complete
 frontier curve further comprises the step of:

filtering the dataset; and

computing the complete frontier curve from the plurality of
 frontier groups.

65. The method of claim **56**, wherein converting the dataset
 comprises the step of:

determining an initial orientation for the dataset; and

wherein computing the complete frontier curve further
 comprises the step of:

reorienting the complete frontier curve to the initial
 orientation.

66. The method of claim **65**, wherein reorienting the complete
 frontier curve comprises the steps of:

transforming the complete frontier curve to the dataset
 center; and rotating the complete frontier curve to the
 initial orientation.

67. The method of claim **56**, wherein computing a complete
 frontier curve further comprises the steps of:

categorizing data from the dataset into hemispheres and
 quadrants;

computing maxima and minima for the variables of the
 dataset;

computing a plurality of frontier curves corresponding to
 the hemispheres and quadrants;

statistically filtering the dataset;

combining the variables into frontier groups, creating composite
 frontier curves;

computing maxima and minima for the composite frontier
 curves; and

combining the composite frontier curves into a complete
 frontier curve.

68. The method of claim **67**, wherein statistically filtering
 the dataset comprises the step of:

removing outlier data points.

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69. A method for generating a complete frontier curve
 comprising the steps of:

providing a dataset of user-selected data corresponding to
 a plurality of reference pharmaceutical units, the user-
 selected data comprising a plurality of variables,
 wherein the plurality of variables comprises one or more
 of:

accident rate, batch quality, number of batches, projected
 yields, actual yields, number of processes, dose
 size production, manufacturing schedules, ingredient
 stocks, ingredient suppliers, number of recalls, work
 shifts, and maintenance costs;

converting the dataset to a geometric coordinate system;
 computing a complete frontier curve for a user-selected
 dataset corresponding to at least one of the plurality of
 variables; and

comparing data corresponding to a target unit to a portion
 of the complete frontier curve.

70. The method of claim **69**, wherein converting the dataset
 further comprises the steps of:

determining an initial orientation for the dataset; and
 rotating the dataset to a predetermined orientation.

71. The method of claim **69**, wherein computing a complete
 frontier curve further comprises the step of
 computing maximum and minimum values for the variables
 of the dataset.

72. The method of claim **69**, further comprising the step of:
 displaying a linear trend of the dataset.

73. The method of claim **69**, further comprising the step of:
 displaying the complete frontier curve.

74. The method of claim **69**, wherein the plurality of variables
 comprises one or more of unit design characteristics,
 operations factors, and maintenance and plant betterment
 data, or combinations thereof.

75. The method of claim **69**, wherein the target unit is a
 reference pharmaceutical unit.

76. The method of claim **69** wherein computing a complete
 frontier curve comprises the step of:

combining data from the dataset into a plurality of frontier
 groups.

77. The method of claim **76**, wherein computing a complete
 frontier curve further comprises the step of:

filtering the dataset; and

computing the complete frontier curve from the plurality of
 frontier groups.

78. The method of claim **69**, wherein converting the dataset
 comprises the step of: determining an initial orientation for
 the dataset; and

wherein computing the complete frontier curve further
 comprises the step of reorienting the complete frontier
 curve to the initial orientation.

79. The method of claim **78**, wherein reorienting the complete
 frontier curve comprises the steps of:

transforming the complete frontier curve to the dataset
 center; and

rotating the complete frontier curve to the initial orientation.

80. The method of claim **69**, wherein computing a complete
 frontier curve further comprises the steps of:

categorizing data from the dataset into hemispheres and
 quadrants;

computing maxima and minima for the variables of the
 dataset;

computing a plurality of frontier curves corresponding to
 the hemispheres and quadrants;

statistically filtering the dataset;

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combining the variables into frontier groups, creating composite frontier curves;
 computing maxima and minima for the composite frontier curves; and combining the composite frontier curves into a complete frontier curve.

81. The method of claim **80**, wherein statistically filtering the dataset comprises the step of:
 removing outlier data points.

82. A method for generating a complete frontier curve comprising the steps of:

providing a dataset of user-selected data corresponding to a plurality of reference healthcare units, the user-selected data comprising a plurality of variables, wherein the plurality of variables comprises one or more of:

total cost of service per year, total expenditure on non-labor inputs, total administrative costs, cost of purchased services, number of patients treated per year by patient category, average length of patient stay, average age of patients, area of specialization, average severity of cases, relative weight of caseload, physician's average age, fraction of caseload with satisfactory outcomes, nursing staff hourly wages, hourly wage for physicians and other professional staff, hourly wage for all other staff, number of beds, number of medical doctors, registered nurses, nonregistered nurses, nurse trainees, therapists, general and other staff, occupancy rate, proportion of patients older than 65, Medicare, Medicaid, private and other patient days, percentage of doctors on staff, rate of hospital admissions per 1000 population, unionization, level of malpractice premiums, percentage of visits using lab tests or x-rays, years of physician experience, number of physicians per 1000 county population, population density, number of acute-care beds, number of long-term beds, number of emergency visits, proportion of female patients, and teaching facilities;

converting the dataset to a geometric coordinate system; computing a complete frontier curve for a user-selected dataset corresponding to at least one of the plurality of variables; and

comparing data corresponding to a target unit to a portion of the complete frontier curve.

83. The method of claim **82**, wherein converting the dataset further comprises the steps of:

determining an initial orientation for the dataset; and rotating the dataset to a predetermined orientation.

84. The method of claim **82**, wherein computing a complete frontier curve further comprises the step of computing maximum and minimum values for the variables of the dataset.

85. The method of claim **82**, further comprising the step of: displaying a linear trend of the dataset.

86. The method of claim **82**, further comprising the step of: displaying the complete frontier curve.

87. The method of claim **82**, wherein the plurality of variables comprises one or more of unit design characteristics, operations factors, and maintenance and plant betterment data, or combinations thereof.

88. The method of claim **82**, wherein the target unit is a reference healthcare unit.

89. The method of claim **82** wherein computing a complete frontier curve comprises the step of:

combining data from the dataset into a plurality of frontier groups.

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90. The method of claim **89**, wherein computing a complete frontier curve further comprises the step of:
 filtering the dataset; and
 computing the complete frontier curve from the plurality of frontier groups.

91. The method of claim **82**, wherein converting the dataset comprises the step of:
 determining an initial orientation for the dataset; and wherein computing the complete frontier curve further comprises the step of reorienting the complete frontier curve to the initial orientation.

92. The method of claim **91**, wherein reorienting the complete frontier curve comprises the steps of:
 transforming the complete frontier curve to the dataset center; and
 rotating the complete frontier curve to the initial orientation.

93. The method of claim **82**, wherein computing a complete frontier curve further comprises the steps of:
 categorizing data from the dataset into hemispheres and quadrants;
 computing maxima and minima for the variables of the dataset; computing a plurality of frontier curves corresponding to the hemispheres and quadrants;
 statistically filtering the dataset;
 combining the variables into frontier groups, creating composite frontier curves;
 computing maxima and minima for the composite frontier curves; and
 combining the composite frontier curves into a complete frontier curve.

94. The method of claim **93**, wherein statistically filtering the dataset comprises the step of:
 removing outlier data points.

95. A method for generating a complete frontier curve comprising the steps of:
 providing a dataset of user-selected data corresponding to a plurality of reference agricultural units, the user-selected data comprising a plurality of variables, wherein the plurality of variables comprises one or more of:

land area dedicated to crops, quantity produced and actually harvested by grain type, labor type, machines, types of fertilizers and nutrient contents, types of pesticides, grain types planted, seeds and seedlings, land rental rates and monthly salaries paid wage earners, types of mechanization available, stocks of tractors and harvesters, available irrigation and water resources, average temperature, average rainfall, degree days compared to a standard measure, length of growing season, altitude, latitude, country, and region;

converting the dataset to a geometric coordinate system; computing a complete frontier curve for a user-selected dataset corresponding to at least one of the plurality of variables; and
 comparing data corresponding to a target unit to a portion of the complete frontier curve.

96. The method of claim **95**, wherein converting the dataset further comprises the steps of:

determining an initial orientation for the dataset; and rotating the dataset to a predetermined orientation.

97. The method of claim **95**, wherein computing a complete frontier curve further comprises the step of:
 computing maximum and minimum values for the variables of the dataset.

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98. The method of claim 95, further comprising the step of: displaying a linear trend of the dataset.

99. The method of claim 95, further comprising the step of: displaying the complete frontier curve.

100. The method of claim 95, wherein the plurality of variables comprises one or more of unit design characteristics, operations factors, and maintenance and plant betterment data, or combinations thereof.

101. The method of claim 95, wherein the target unit is a reference agricultural unit.

102. The method of claim 95 wherein computing a complete frontier curve comprises the step of: combining data from the dataset into a plurality of frontier groups.

103. The method of claim 102, wherein computing a complete frontier curve further comprises the step of: filtering the dataset; and computing the complete frontier curve from the plurality of frontier groups.

104. The method of claim 95, wherein converting the dataset comprises the step of: determining an initial orientation for the dataset; and wherein computing the complete frontier curve further comprises the step of: reorienting the complete frontier curve to the initial orientation.

105. The method of claim 104, wherein reorienting the complete frontier curve comprises the steps of: transforming the complete frontier curve to the dataset center; and rotating the complete frontier curve to the initial orientation.

106. The method of claim 95, wherein computing a complete frontier curve further comprises the steps of: categorizing data from the dataset into hemispheres and quadrants; computing maxima and minima for the variables of the dataset; computing a plurality of frontier curves corresponding to the hemispheres and quadrants; statistically filtering the dataset; combining the variables into frontier groups, creating composite frontier curves; computing maxima and minima for the composite frontier curves; and combining the composite frontier curves into a complete frontier curve.

107. The method of claim 106, wherein statistically filtering the dataset comprises the step of: removing outlier data points.

108. A method for generating a complete frontier curve comprising the steps of: providing a dataset of user-selected data corresponding to a plurality of reference environmental units, the user-selected data comprising a plurality of variables, wherein the plurality of variables comprises one or more of ratio of area of disturbed land to total area, total linear edge between natural land cover and human land use, ratio of average patch size to the maximum possible, proportion of endangered species to total individual species, mortality in growing stock on timberlands, ratio of actual productivity on timberlands to potential productivity, absolute value of the difference between recent stream flow and historical average, total nitrogen measured in surface waters, maximum pH in precipitation minus observed pH in precipitation, total phosphorous measured in surface waters, total toxic

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chemical releases to the environment (air, water, and land), proportion of area that is designated as protected, human population density, dam density, beef cattle density, mining density, productive oil and gas well density, timber harvest, mad density, outdoor recreation activity measures, total farm production, mean annual temperature, spatial variation in temperature, seasonal variation in temperature, mean annual precipitation, seasonal variation in precipitation, spatial variation in precipitation, and total vegetation carbon;

converting the dataset to a geometric coordinate system; computing a complete frontier curve for a user-selected dataset corresponding to at least one of the plurality of variables; and comparing data corresponding to a target unit to a portion of the complete frontier curve.

109. The method of claim 108, wherein converting the dataset further comprises the steps of: determining an initial orientation for the dataset; and rotating the dataset to a predetermined orientation.

110. The method of claim 108, wherein computing a complete frontier curve further comprises the step of: computing maximum and minimum values for the variables of the dataset.

111. The method of claim 108, further comprising the step of: displaying a linear trend of the dataset.

112. The method of claim 108, further comprising the step of: displaying the complete frontier curve.

113. The method of claim 108, wherein the plurality of variables comprises one or more of unit design characteristics, operations factors, and maintenance and plant betterment data, or combinations thereof.

114. The method of claim 108, wherein the target unit is a reference environmental unit.

115. The method of claim 108 wherein computing a complete frontier curve comprises the step of: combining data from the dataset into a plurality of frontier groups.

116. The method of claim 115, wherein computing a complete frontier curve further comprises the step of: filtering the dataset; and computing the complete frontier curve from the plurality of frontier groups.

117. The method of claim 108, wherein converting the dataset comprises the step of: determining an initial orientation for the dataset; and wherein computing the complete frontier curve further comprises the step of: reorienting the complete frontier curve to the initial orientation.

118. The method of claim 117, wherein reorienting the complete frontier curve comprises the steps of: transforming the complete frontier curve to the dataset center; and rotating the complete frontier curve to the initial orientation.

119. The method of claim 108, wherein computing a complete frontier curve further comprises the steps of: categorizing data from the dataset into hemispheres and quadrants; computing maxima and minima for the variables of the dataset; computing a plurality of frontier curves corresponding to the hemispheres and quadrants; statistically filtering the dataset;

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combining the variables into frontier groups, creating composite frontier curves;
 computing maxima and minima for the composite frontier curves; and
 combining the composite frontier curves into a complete frontier curve.

120. The method of claim **119**, wherein statistically filtering the dataset comprises the step of:
 removing outlier data points.

121. A method for generating a complete frontier curve comprising the steps of:

providing a dataset of user-selected data corresponding to a plurality of reference offshore energy production units, the user-selected data comprising a plurality of variables,

wherein the plurality of variables comprises one or more of:

offshore drilling costs grouped by depth intervals, operating costs for each platform, monthly oil output, monthly gas output, produced water, platform size, platform water depth, oil reserve size, gas reserve size, reservoir-level porosity, oil output, gas output, produced water output, quantity of fluid injected, number of exploration wells drilled, total drilling distance of exploration wells, total vertical distance of exploration wells, number of development wells drilled, total drilling distance of development wells, total vertical distance of development wells, number of platforms, total number of slots, total number of slots drilled, water depth, oil reserves, gas reserves, original proved oil and gas combined reserves, number of environmental regulations, environmental compliance costs, and environmental emissions;

converting the dataset to a geometric coordinate system;
 computing a complete frontier curve for a user-selected dataset corresponding to at least one of the plurality of variables; and

comparing data corresponding to a target unit to a portion of the complete frontier curve.

122. The method of claim **121**, wherein converting the dataset further comprises the steps of:

determining an initial orientation for the dataset; and
 rotating the dataset to a predetermined orientation.

123. The method of claim **121**, wherein computing a complete frontier curve further comprises the step of:

computing maximum and minimum values for the variables of the dataset.

124. The method of claim **121**, further comprising the step of:

displaying a linear trend of the dataset.

125. The method of claim **121**, further comprising the step of:

displaying the complete frontier curve.

126. The method of claim **121**, wherein the plurality of variables comprises one or more of unit design characteristics, operations factors, and maintenance and plant betterment data, or combinations thereof.

127. The method of claim **121**, wherein the target unit is a reference offshore energy production unit.

128. The method of claim **121** wherein computing a complete frontier curve comprises the step of:

combining data from the dataset into a plurality of frontier groups.

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129. The method of claim **128**, wherein computing a complete frontier curve further comprises the step of:
 filtering the dataset; and
 computing the complete frontier curve from the plurality of frontier groups.

130. The method of claim **121**, wherein converting the dataset comprises the step of:
 determining an initial orientation for the dataset; and
 wherein computing the complete frontier curve further comprises the step of:
 reorienting the complete frontier curve to the initial orientation.

131. The method of claim **130**, wherein reorienting the complete frontier curve comprises the steps of:
 transforming the complete frontier curve to the dataset center; and
 rotating the complete frontier curve to the initial orientation.

132. The method of claim **121**, wherein computing a complete frontier curve further comprises the steps of
 categorizing data from the dataset into hemispheres and quadrants;
 computing maxima and minima for the variables of the dataset;
 computing a plurality of frontier curves corresponding to the hemispheres and quadrants;
 statistically filtering the dataset;
 combining the variables into frontier groups, creating composite frontier curves;
 computing maxima and minima for the composite frontier curves; and
 combining the composite frontier curves into a complete frontier curve.

133. The method of claim **132**, wherein statistically filtering the dataset comprises the step of:
 removing outlier data points.

134. A method for generating a complete frontier curve comprising the steps of

providing a dataset of user-selected data corresponding to a plurality of reference educational units, the user-selected data comprising a plurality of variables,
 wherein the plurality of variables comprises one or more of:

school district, state, population in district, average family income in district, average level of education of school district population, average performance on several standardized tests by grade level, number of classroom days in the school year, instructional expenditures per student, other expenditures per student, average teacher salary, average years of experience for teachers, proportion of teachers having an advanced degree, student-teacher ratio, total enrollment in school, percent of students eligible for subsidized lunches, percent minority students, percent of students classified as possessing English proficiency, number of teachers, number of teacher aides, ratio of administrative staff to teaching staff, expenditures per student for administrative and other school operations, district school taxes per student, and average administrative salary;

converting the dataset to a geometric coordinate system;
 computing a complete frontier curve for a user-selected dataset corresponding to at least one of the plurality of variables; and
 comparing data corresponding to a target unit to a portion of the complete frontier curve.

135. The method of claim 134, wherein converting the dataset further comprises the steps of:

determining an initial orientation for the dataset; and rotating the dataset to a predetermined orientation.

136. The method of claim 134, wherein computing a complete frontier curve further comprises the step of:

computing maximum and minimum values for the variables of the dataset.

137. The method of claim 134, further comprising the step of:

displaying a linear trend of the dataset.

138. The method of claim 134, further comprising the step of:

displaying the complete frontier curve.

139. The method of claim 134, wherein the plurality of variables comprises one or more of unit design characteristics, operations factors, and maintenance and plant betterment data, or combinations thereof.

140. The method of claim 134, wherein the target unit is a reference educational unit.

141. The method of claim 134 wherein computing a complete frontier curve comprises the step of:

combining data from the dataset into a plurality of frontier groups.

142. The method of claim 141, wherein computing a complete frontier curve further comprises the step of:

filtering the dataset; and computing the complete frontier curve from the plurality of frontier groups.

143. The method of claim 134, wherein converting the dataset comprises the step of

determining an initial orientation for the dataset; and wherein computing the complete frontier curve further comprises the step of: reorienting the complete frontier curve to the initial orientation.

144. The method of claim 143, wherein reorienting the complete frontier curve comprises the steps of:

transforming the complete frontier curve to the dataset center; and rotating the complete frontier curve to the initial orientation.

145. The method of claim 134, wherein computing a complete frontier curve further comprises the steps of:

categorizing data from the dataset into hemispheres and quadrants;

computing maxima and minima for the variables of the dataset;

computing a plurality of frontier curves corresponding to the hemispheres and quadrants;

statistically filtering the dataset;

combining the variables into frontier groups, creating composite frontier curves;

computing maxima and minima for the composite frontier curves; and

combining the composite frontier curves into a complete frontier curve.

146. The method of claim 145, wherein statistically filtering the dataset comprises the step of:

removing outlier data points.

147. A method for generating an individual frontier curve comprising the steps of:

providing a dataset of user-selected data corresponding to a plurality of reference units, the user-selected data comprising a plurality of variables;

converting the dataset to a geometric coordinate system; computing a complete frontier curve for a user-selected dataset corresponding to at least one of the plurality of variables.

148. The method of claim 147, further comprising the step of:

comparing data corresponding to a target unit to a portion of the individual frontier curve.

149. The method of claim 147, wherein the plurality of units is selected from a set of unit types consisting of:

power generating, refining, pipeline, chemical, industrial, pharmaceutical, healthcare, agricultural, environmental, offshore, and educational units.

150. The method of claim 147, wherein computing an individual frontier curve further comprises the step of:

computing the individual frontier curve from the plurality of frontier groups.

151. The method of claim 147, wherein computing an individual frontier curve further comprises the step of:

computing maximum and minimum values for the variables of the dataset.

152. A system comprising:

a server, comprising:

a processor, and a storage subsystem;

a database stored by the storage subsystem comprising a plurality of data corresponding to units; and

a computer program stored by the storage subsystem that, when executed, causes the processor to:

select a dataset from the plurality of data; convert the dataset to a geometric coordinate system; compute a complete frontier curve based on the dataset.

153. The system of claim 152, wherein the computer program, when executed further causes the processor to compare data of a target unit with a portion of the complete frontier curve.

154. The system of claim 152, wherein the plurality of data corresponding to units is selected from a set of unit types consisting of: power generating, refining, pipeline, chemical, industrial, pharmaceutical, healthcare, agricultural, environmental, offshore, and educational units.

155. The system of claim 152, wherein to compute the complete frontier curve, the computer program, when executed further causes the processor to:

combine data from the dataset into a plurality of frontier groups.

156. The system of claim 152, wherein the computer program, when executed further causes the processor to:

filter the dataset; and

compute the complete frontier curve from the plurality of frontier groups.

157. The system of claim 152, wherein to convert the dataset, the computer program, when executed further causes the processor to:

determine an initial orientation for the dataset; and rotate the dataset to a predetermined orientation.

158. The system of claim 152, wherein to compute the complete frontier curve, the computer program, when executed further causes the processor to:

compute maximum and minimum values for the variables of the dataset.

159. The system of claim 152, wherein to compute the complete frontier curve, the computer program, when executed further causes the processor to:

categorize data from the dataset into hemispheres and quadrants;

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compute maxima and minima for the variables of the dataset;
 compute a plurality of frontier curves corresponding to the hemispheres and quadrants;
 statistically filtering the dataset;
 combine the variables into frontier groups, creating composite frontier curves;
 compute maxima and minima for the composite frontier curves; and
 combine the composite frontier curves into a complete frontier curve. 10

160. The system of claim 152, wherein to convert the dataset, the computer program, when executed further causes the processor to:
 determine an initial orientation for the dataset; and 15
 wherein computing the complete frontier curve further comprises the step of reorienting the complete frontier curve to the initial orientation.

161. The system of claim 160, wherein to reorient the complete frontier curve, the computer program, when executed further causes the processor to: 20
 transform the complete frontier curve to the dataset center; and
 rotate the complete frontier curve to the initial orientation.

162. A system comprising: 25
 a server, comprising:
 a processor, and
 a storage subsystem;
 a database stored by the storage subsystem comprising a plurality of data corresponding to units; and 30
 a computer program stored by the storage subsystem that, when executed, causes the processor to:
 select a dataset from the plurality of data;
 convert the dataset to a geometric coordinate system;
 compute an individual frontier curve based on the dataset. 35

163. The system of claim 162, wherein the computer program, when executed further causes the processor to compare data of a target unit with a portion of the individual frontier curve.

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164. The system of claim 162, wherein the plurality of data corresponding to units is selected from a set of unit types consisting of: power generating, refining, pipeline, chemical, industrial, pharmaceutical, healthcare, agricultural, environmental, offshore, and educational units. 5

165. The system of claim 162, wherein to compute the individual frontier curve, the computer program, when executed further causes the processor to:
 combine data from the dataset into a plurality of frontier groups.

166. The system of claim 162, wherein the computer program, when executed further causes the processor to:
 filter the dataset; and
 compute the individual frontier curves from the plurality of frontier groups.

167. The system of claim 162, wherein to convert the dataset, the computer program, when executed further causes the processor to:
 determine an initial orientation for the dataset; and
 rotate the dataset to a predetermined orientation.

168. The system of claim 162, wherein to compute the individual frontier curve, the computer program, when executed further causes the processor to:
 compute maximum and minimum values for the variables of the dataset.

169. The system of claim 162, wherein to convert the dataset, the computer program, when executed further causes the processor to:
 determine an initial orientation for the dataset; and
 wherein computing the individual frontier curve further comprises the step of reorienting the individual frontier curve to the initial orientation.

170. The system of claim 169, wherein to reorient the individual frontier curve, the computer program, when executed further causes the processor to:
 transform the individual frontier curve to the dataset center; and
 rotate the individual frontier curve to the initial orientation.

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